

Theoretical Particle Physics

(Theorie Elementarteilchen)

Vladimir Pascalutsa

**Institute of Nuclear Physics & Cluster of Excellence PRISMA,
University of Mainz, Germany**



Module Topical Courses: “Theoretical Particle Physics”

ID number (JOGU-StINe) 08.128.809	Workload (workload) 180 h	Course Duration (laut Studienverlaufsplan) 1	Designated term (laut Studienverlaufsplan) 1	Credit Points (LP) 6 LP
1.	Courses/Teaching methods Lecture with excercises “Theoretical Particle Physics” (WP) Lecture (WP) Excercises (WP)	Contact time 3 SWS/31.5 h 1 SWS/10.5 h	Self-study 138 h	Credit Points 6 LP
2.	Group sizes Lecture: unlimited Excercises: 20			
3.	Qualification and program goals / Competences The lecture course “Theoretical Particle Physics” builds upon and continues the lecture course “Relativistic Quantum Field Theory”. The lectures’ program goal is to provide a basic understanding of concepts and methods of quantum field theory which are required for a MA thesis in theoretical particle physics.			
4.	Course content Path integral formalism, quantum corrections, renormalization in QED, renormalization group; non-Abelian gauge theories, quantum chromodynamics (QCD), spontaneous symmetry breaking, Higgs mechanism, standard model of particle physics.			
5.	Applicable to the following programs MSc. Physics			
6.	Recommended prerequisites			
7.	Entry requirements			
8.	Mode and duration of examinations <i>8.1 Active participation</i> successful completion of the excercises <i>8.2 Course achievements</i> <i>8.3 Module examination</i> Common oral examination (30 – 45 Min.) covering two topical courses			
9.	Weighting of the achievement in the overall grade 6/120			
10.	Module frequency Usually every semester			
11.	Persons responsible for this module and full-time lecturers Responsible: Prof. Dr. S. Weinzierl Lecturers: All professors of theoretical high energy physics			
12.	Auxiliary Information Course language: English Literature: Peskin & Schroeder, Ryder, Schwartz, Zee			

First glimpse of
the Standard Model
of Particle Physics

Fundamental constants of the vacuum

$$\hbar \simeq 6.58 \times 10^{-16} \text{ eV s}$$

$$c \simeq 3 \cdot 10^8 \text{ m/s}$$

quantum physics

special relativity



Quantum Field Theory

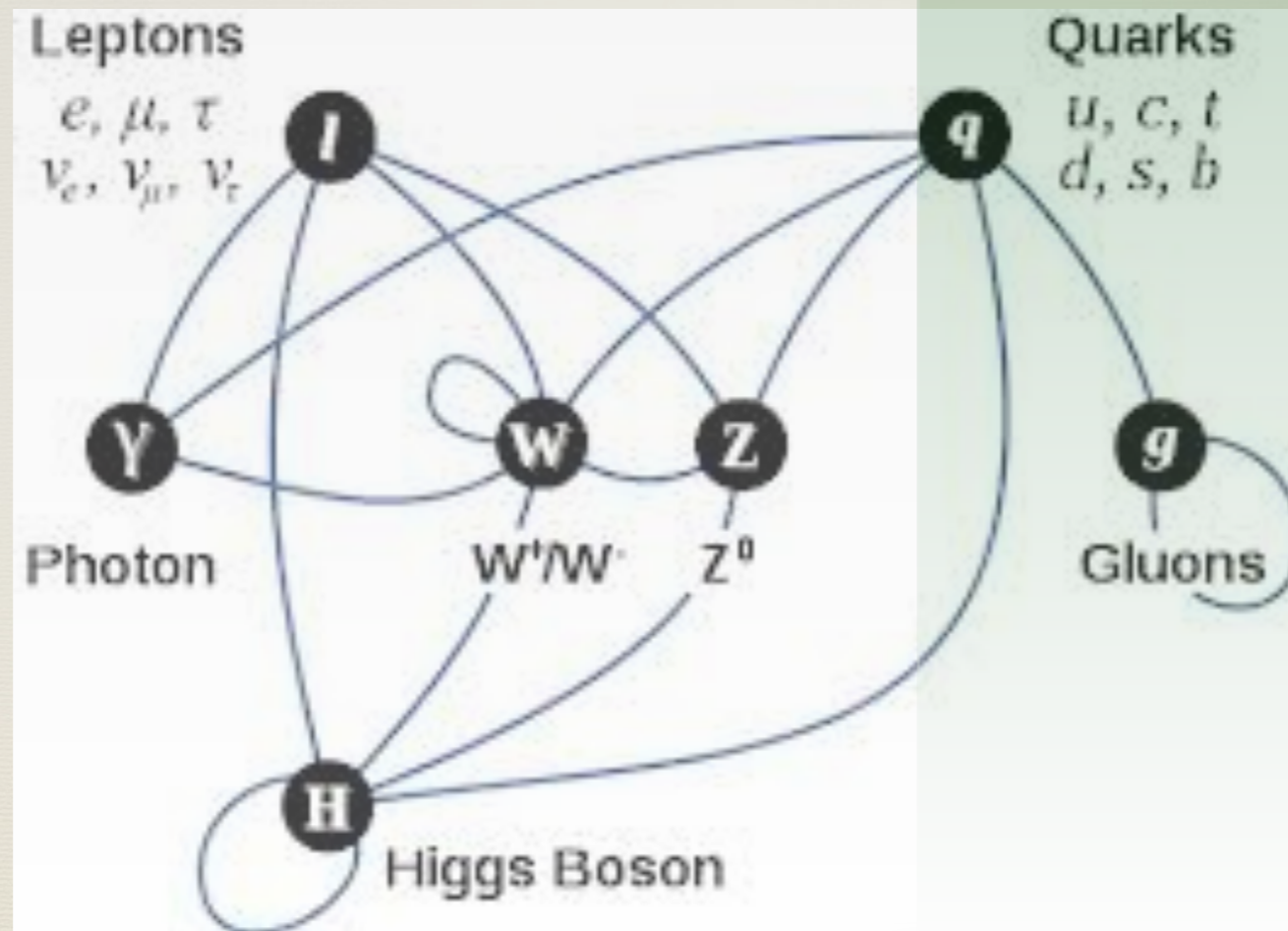
$$\hbar = c = 1 \text{ (Natural Units)}, \quad \text{e.g. } E = \sqrt{m^2 + p^2}, \quad \alpha = \frac{e^2}{4\pi} \simeq \frac{1}{137.036}$$

$$\hbar c = 0.1973\dots \text{ GeV fm} = 0.1973\dots \text{ eV } \mu\text{m}$$

Standard Model

Electroweak

QCD

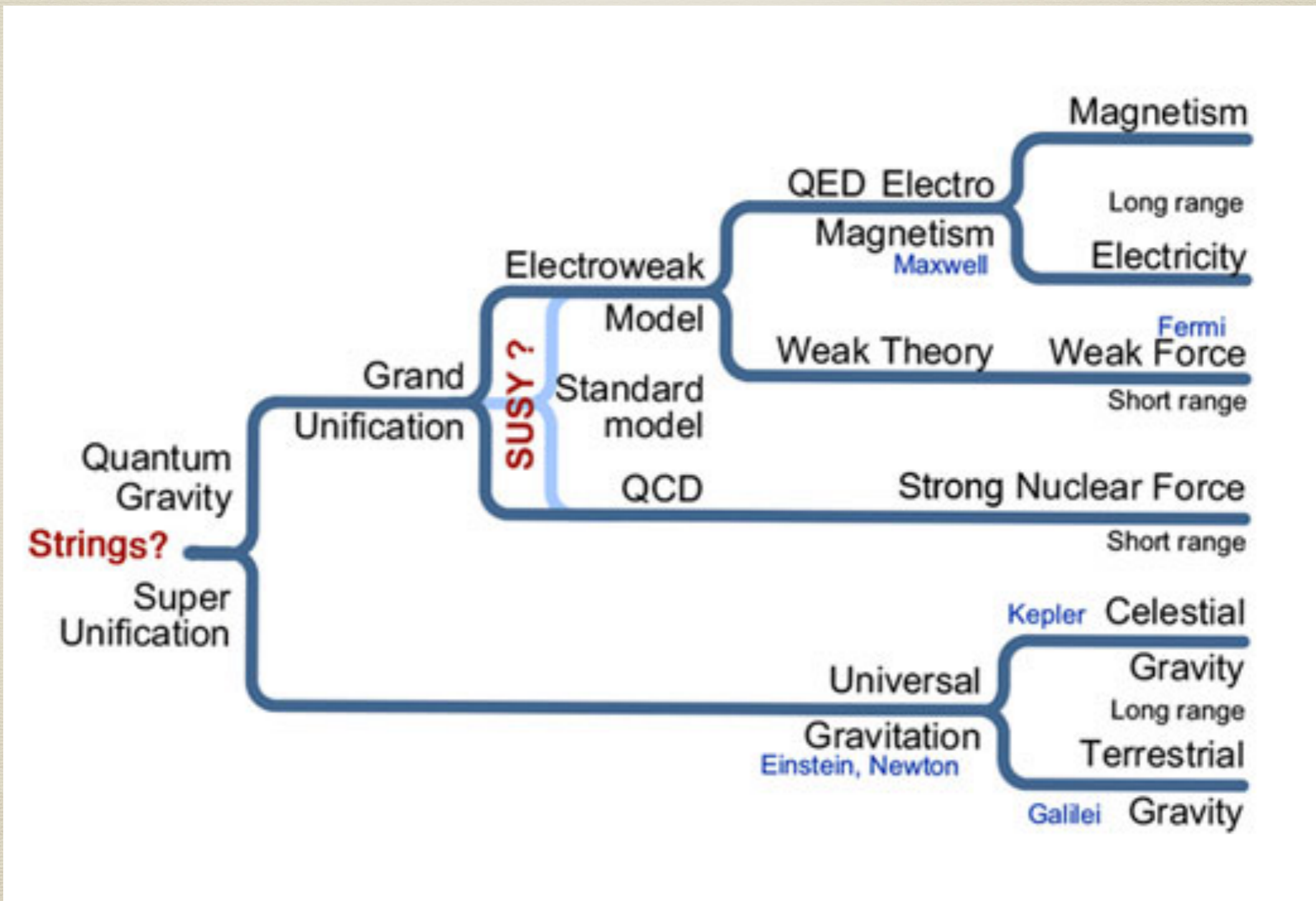


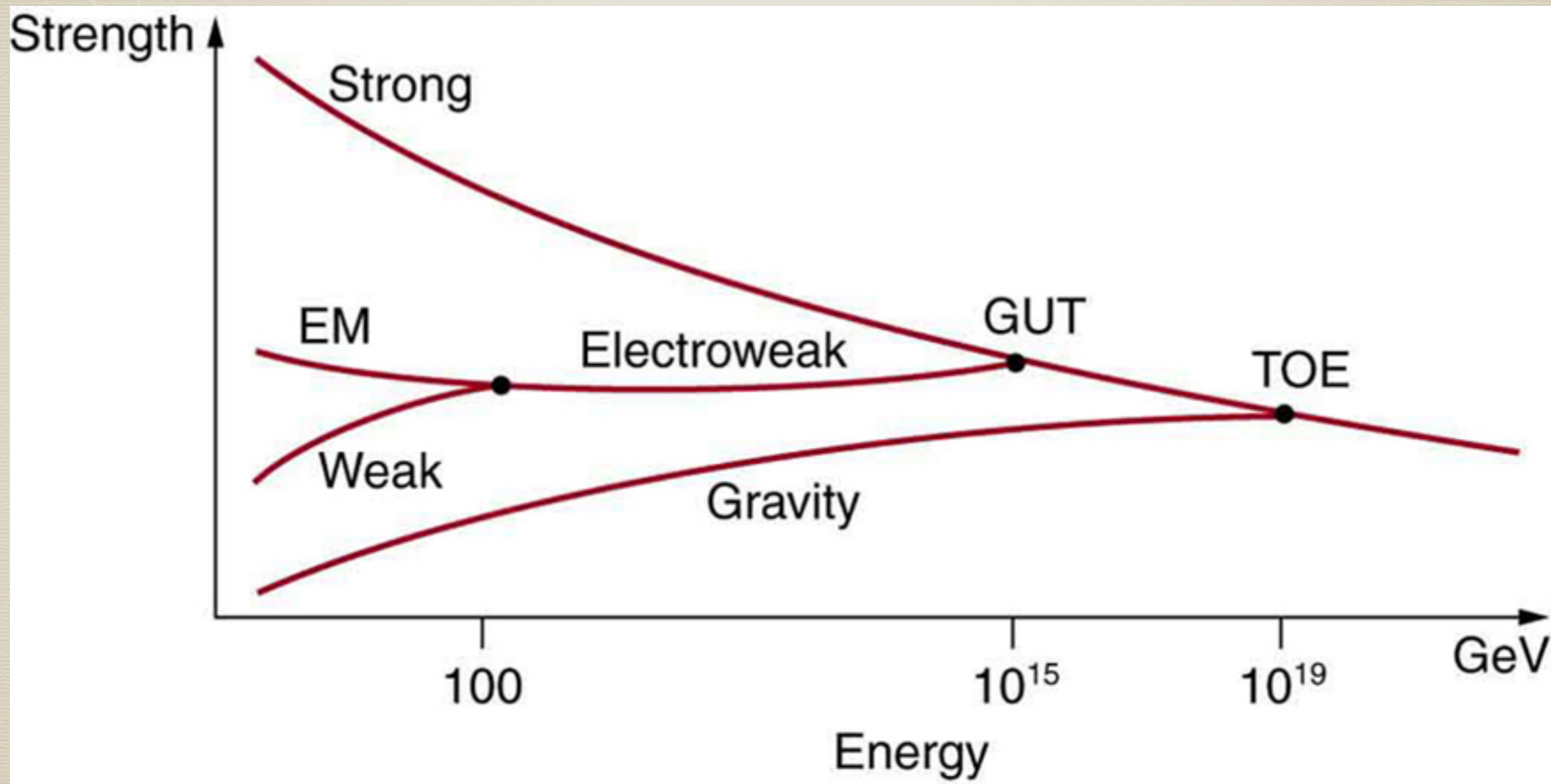
$S = 1/2$, spinor : $\psi^{(\alpha)}(x)$

$S = 1$, vector : $A_\mu(x)$

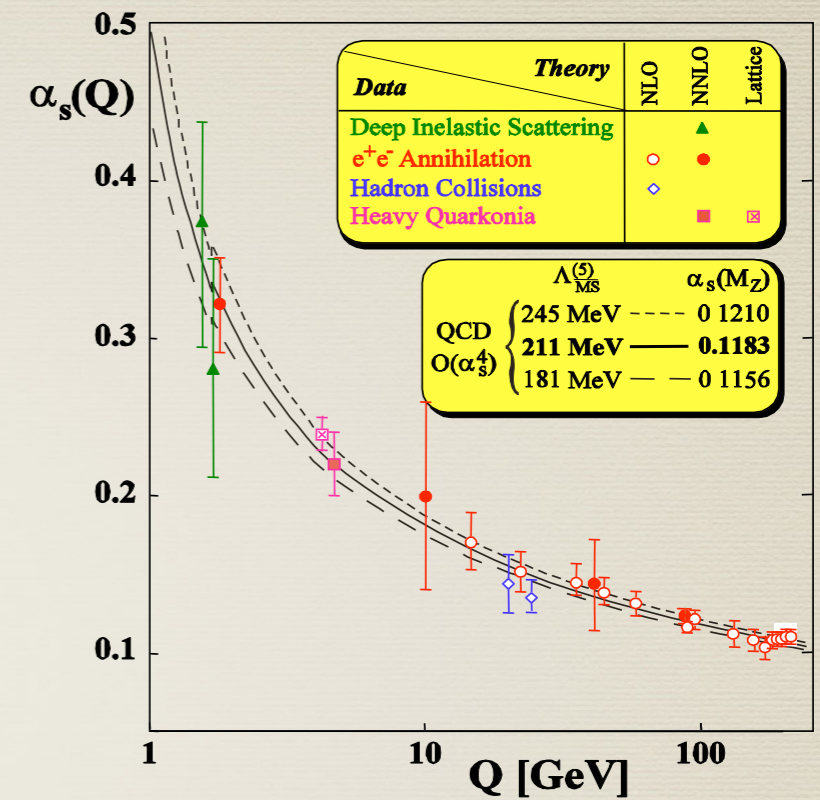
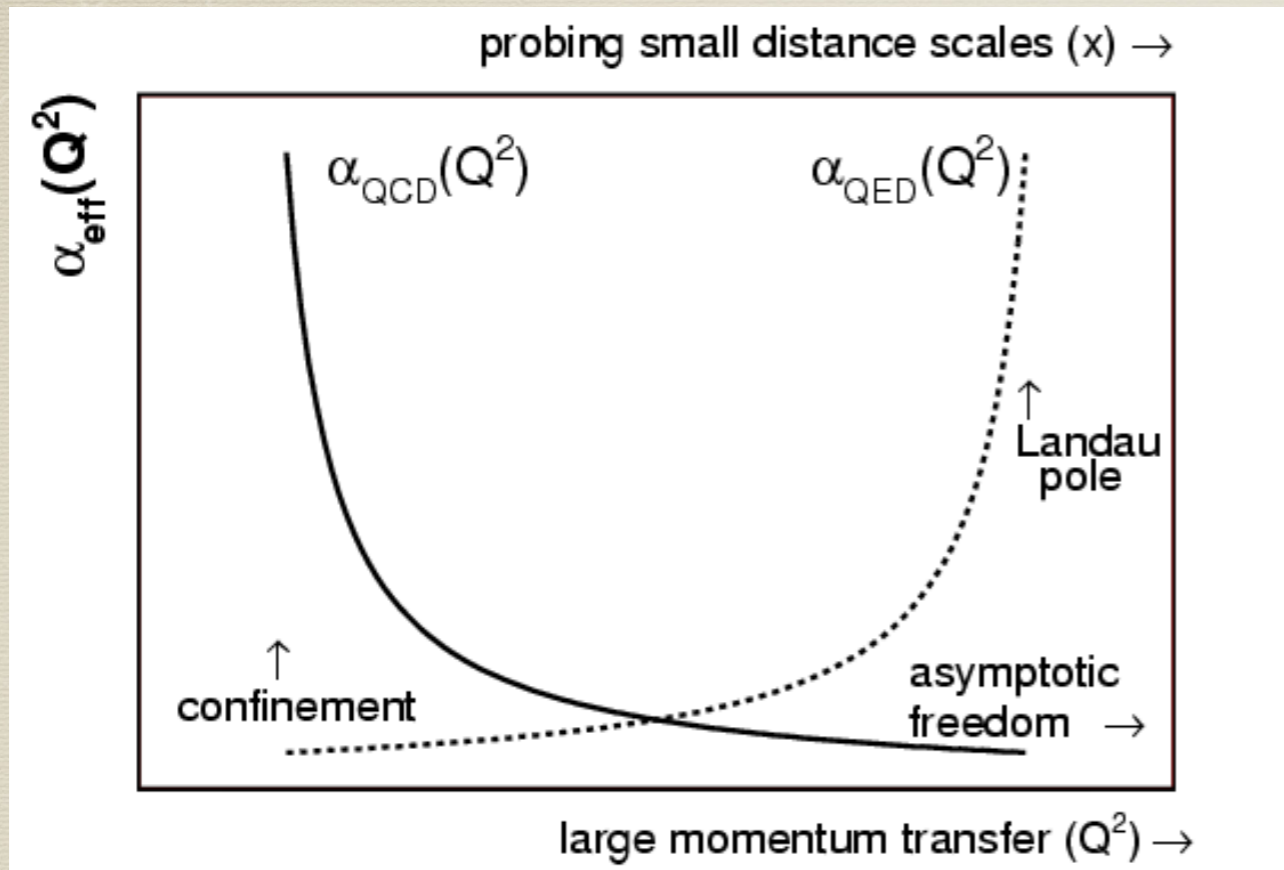
$S = 0$, scalar : $\phi(x)$

Unification of fundamental interactions



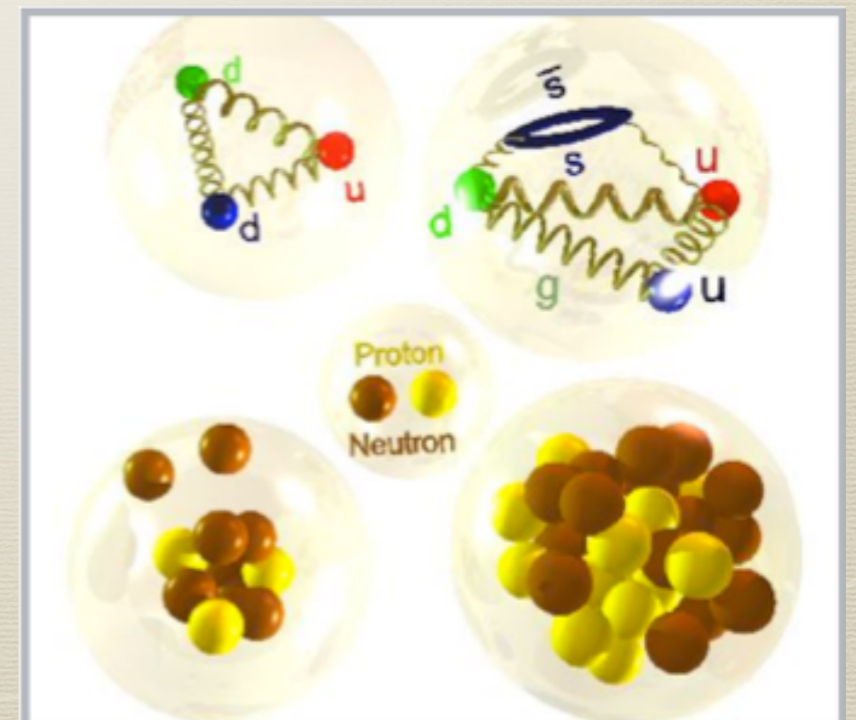


Running of QCD coupling



For $Q^2 \rightarrow \infty$, $\alpha_s \rightarrow 0$: **asymptotic freedom**

For $Q \sim \Lambda_{QCD}$ non-perturbative phenomena:
color confinement,
spontaneous chiral symmetry breaking,
generation of nucleon mass, ...



Feynman rules of the SM

([arXiv: hep-ph/9507456](https://arxiv.org/abs/hep-ph/9507456))

Propagators:

$$\begin{array}{c} W_\mu^+ \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} W_\nu^- \\ \bullet \end{array} \quad \frac{1}{k^2 - M_W^2 + i\epsilon} \left(g_{\mu\nu} - (1 - \xi_W) \frac{k_\mu k_\nu}{k^2 - \xi_W M_W^2 + i\epsilon} \right)$$

$$\begin{array}{c} Z_\mu \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} Z_\nu \\ \bullet \end{array} \quad \frac{1}{k^2 - M_Z^2 + i\epsilon} \left(g_{\mu\nu} - (1 - \xi_Z) \frac{k_\mu k_\nu}{k^2 - \xi_Z M_Z^2 + i\epsilon} \right)$$

$$\begin{array}{c} A_\mu \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} A_\nu \\ \bullet \end{array} \quad \frac{1}{k^2 + i\epsilon} \left(g_{\mu\nu} - (1 - \xi_A) \frac{k_\mu k_\nu}{k^2 + i\epsilon} \right)$$

$$\begin{array}{c} G_\mu^a \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} G_\nu^b \\ \bullet \end{array} \quad \delta^{ab} \frac{1}{k^2 + i\epsilon} \left(g_{\mu\nu} - (1 - \xi_G) \frac{k_\mu k_\nu}{k^2 + i\epsilon} \right)$$

$$\begin{array}{c} \psi \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} \bar{\psi} \\ \bullet \end{array} \quad \frac{\hat{k} + m}{k^2 - m^2 + i\epsilon} = \frac{\hat{k} + m}{m^2 - k^2 + i\epsilon}$$

$$\begin{array}{c} \phi \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} \phi \\ \bullet \end{array} \quad - \frac{1}{k^2 - m_H^2 + i\epsilon}$$

$$\begin{array}{c} \omega^+ \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} \omega^- \\ \bullet \end{array} \quad - \frac{1}{k^2 - \xi_W m_W^2 + i\epsilon}$$

$$\begin{array}{c} z \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} z \\ \bullet \end{array} \quad - \frac{1}{k^2 - \xi_Z m_Z^2 + i\epsilon}$$

$$\begin{array}{c} c^+ \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} \bar{c}^- \\ \bullet \end{array} \quad - \frac{1}{k^2 - \xi_W m_W^2 + i\epsilon}$$

$$\begin{array}{c} c^- \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} \bar{c}^+ \\ \bullet \end{array} \quad - \frac{1}{k^2 - \xi_W m_W^2 + i\epsilon}$$

$$\begin{array}{c} c^Z \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} \bar{c}^Z \\ \bullet \end{array} \quad - \frac{1}{k^2 - \xi_Z m_Z^2 + i\epsilon}$$

$$\begin{array}{c} c^A \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} \bar{c}^A \\ \bullet \end{array} \quad - \frac{1}{k^2 + i\epsilon}$$

$$\begin{array}{c} c_a \\ \bullet \end{array} \begin{array}{c} \leftarrow \\ \text{---} \\ \bullet \end{array} \begin{array}{c} \bar{c}_b \\ \bullet \end{array} \quad - \delta_{ab} \frac{1}{k^2 + i\epsilon}$$

Vertices

10.4.1 Gauge Boson Three-vertices

ZW^+W^-

$$e \cot \vartheta_W \left((k-p)^\gamma g^{\alpha\beta} + (p-q)^\alpha g^{\beta\gamma} + (q-k)^\beta g^{\gamma\alpha} \right)$$

AW^+W^-

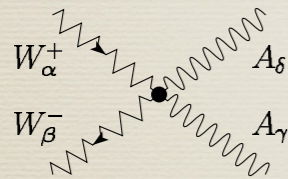
$$e \left((k-p)^\gamma g^{\alpha\beta} + (p-q)^\alpha g^{\beta\gamma} + (q-k)^\beta g^{\gamma\alpha} \right)$$

GGG

$$ig_s f^{abc} \left((p-k)^\gamma g^{\alpha\beta} + (q-p)^\alpha g^{\beta\gamma} + (k-q)^\beta g^{\gamma\alpha} \right)$$

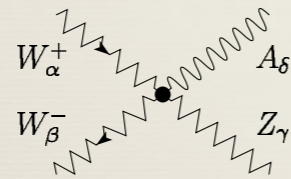
10.4.2 Gauge Boson Four-vertices

AAW^+W^-



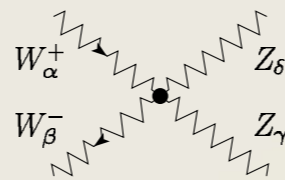
$$e^2 (g^{\alpha\gamma} g^{\beta\delta} + g^{\alpha\delta} g^{\beta\gamma} - 2g^{\alpha\beta} g^{\gamma\delta})$$

AZW^+W^-



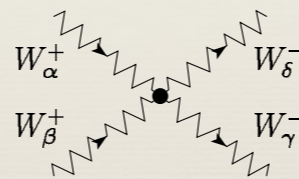
$$e^2 \cot \vartheta_W (g^{\alpha\gamma} g^{\beta\delta} + g^{\alpha\delta} g^{\beta\gamma} - 2g^{\alpha\beta} g^{\gamma\delta})$$

ZZW^+W^-



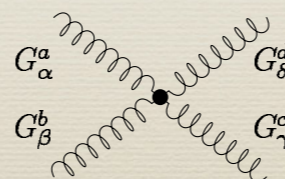
$$e^2 \cot^2 \vartheta_W (g^{\alpha\gamma} g^{\beta\delta} + g^{\alpha\delta} g^{\beta\gamma} - 2g^{\alpha\beta} g^{\gamma\delta})$$

$W^+W^-W^+W^-$



$$-\frac{e^2}{\sin^2 \vartheta_W} (g^{\alpha\gamma} g^{\beta\delta} + g^{\alpha\delta} g^{\beta\gamma} - 2g^{\alpha\beta} g^{\gamma\delta})$$

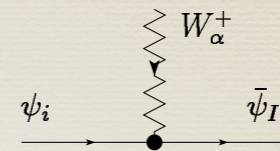
$GGGG$



$$-g_s^2 \left(f^{ab} f^{cd} (g^{\alpha\gamma} g^{\beta\delta} - g^{\alpha\delta} g^{\beta\gamma}) + f^{ac} f^{db} (g^{\alpha\delta} g^{\beta\gamma} - g^{\alpha\beta} g^{\gamma\delta}) + f^{ad} f^{bc} (g^{\alpha\beta} g^{\gamma\delta} - g^{\alpha\gamma} g^{\delta\beta}) \right)$$

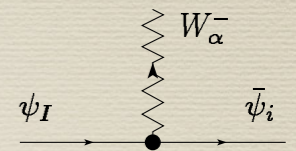
10.4.3 Gauge-boson-fermion Vertices

$\bar{\psi}_I \psi_i W^+$



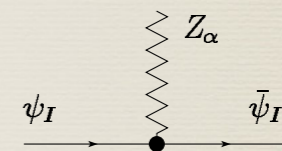
$$\frac{e}{2\sqrt{2} \sin \vartheta_W} V_{iI}^+ \gamma^\alpha (1 - \gamma^5)$$

$\bar{\psi}_i \psi_I W^-$



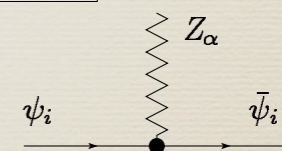
$$\frac{e}{2\sqrt{2} \sin \vartheta_W} V_{iI}^- \gamma^\alpha (1 - \gamma^5)$$

$\bar{\psi}_I \psi_I Z$



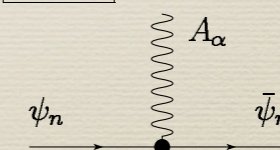
$$\frac{e}{\sin 2\vartheta_W} \gamma^\alpha \left(\frac{1}{2}(1 - \gamma^5) - 2Q_I \sin^2 \vartheta_W \right)$$

$\bar{\psi}_i \psi_i Z$



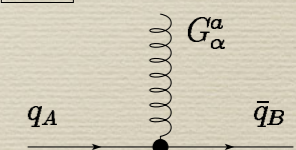
$$\frac{e}{\sin 2\vartheta_W} \gamma^\alpha \left(-\frac{1}{2}(1 - \gamma^5) - 2Q_i \sin^2 \vartheta_W \right)$$

$\bar{\psi}_n \psi_n A$



$$e Q_n \gamma^\alpha \quad (n = i, I)$$

$\bar{q}_q G$

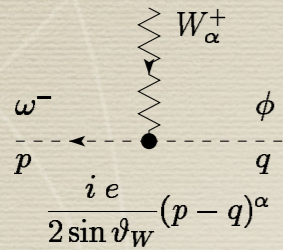


$$g_s (t^a)_{BA} \gamma^\alpha$$

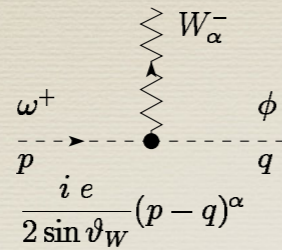
Vertices (continued)

10.4.4 Gauge-boson-Higgs Three-vertices

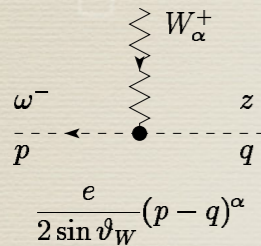
$\phi \omega^- W^+$



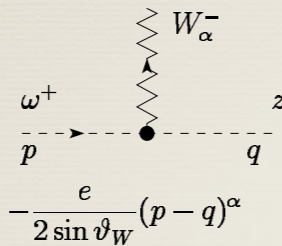
$\phi \omega^+ W^-$



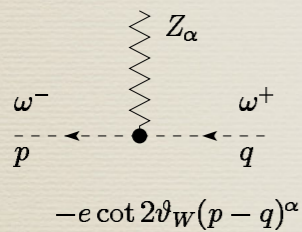
$z \omega^- W^+$



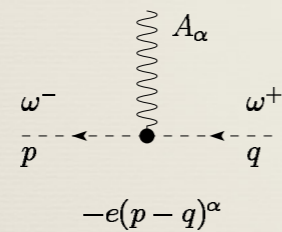
$z \omega^+ W^-$



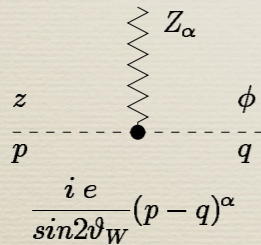
$\omega^+ \omega^- Z$



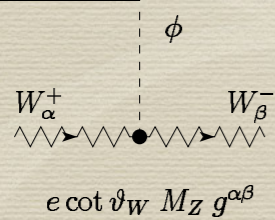
$\omega^+ \omega^- A$



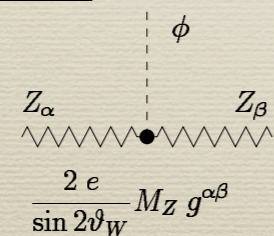
$\phi z Z$



$\phi W^+ W^-$

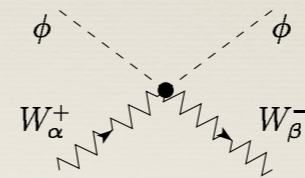


$\phi Z Z$

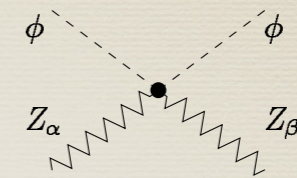


10.4.5 Gauge-boson-Higgs Four-vertices

$\phi \phi W^+ W^-$



$\phi \phi Z Z$

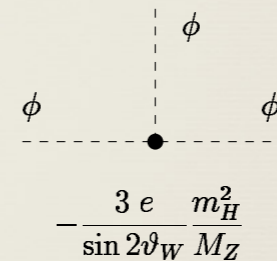


$$\frac{e^2}{2 \sin^2 \vartheta_W} g^{\alpha\beta}$$

$$\frac{2 e^2}{\sin^2 2\vartheta_W} g^{\alpha\beta}$$

10.4.6 Higgs Three-vertices

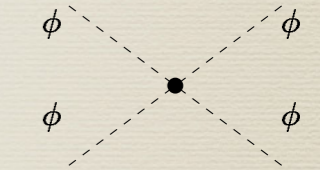
$\phi \phi \phi$



$$-\frac{3 e m_H^2}{\sin 2\vartheta_W M_Z}$$

10.4.7 Higgs Four-vertices

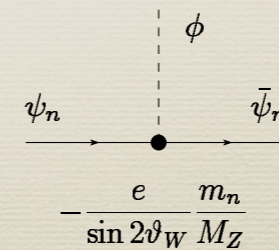
$\phi \phi \phi \phi$



$$-\frac{3 e^2 m_H^2}{\sin^2 2\vartheta_W M_Z^2}$$

10.4.8 Higgs-boson-fermion Vertices

$\bar{\psi}_n \psi_n \phi$



$$-\frac{e m_n}{\sin 2\vartheta_W M_Z}$$

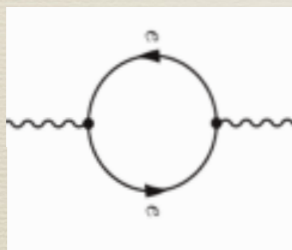
Loops

Finally, every loop integration is performed by the rule

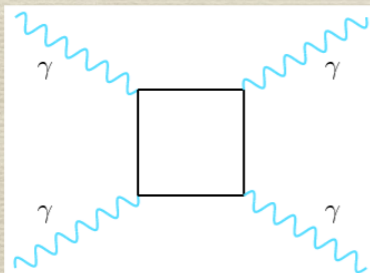
$$\int \frac{d^d k}{i(2\pi)^d},$$

and with every fermion or ghost loop we associate extra factor (-1) .

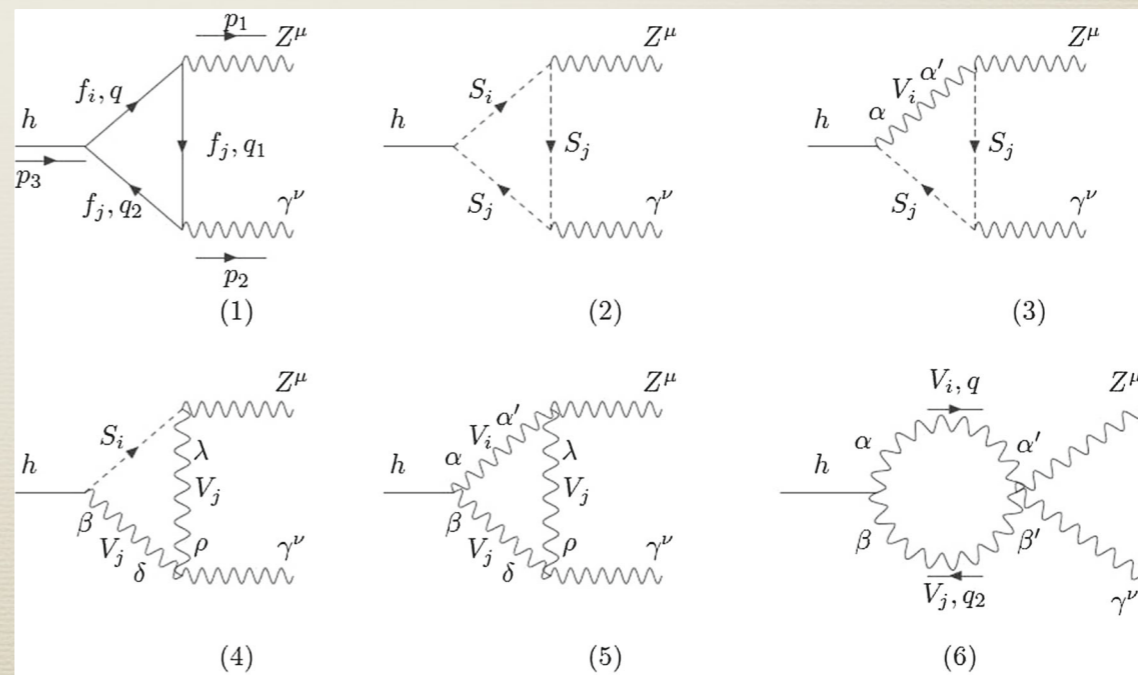
Vacuum polarization



Light-by-light scattering



Higgs decay



Exercise sessions

will sometimes involve computer algebra,
i.e., FORM, FeynCalc, LoopTools (Mathematica)

BYOL